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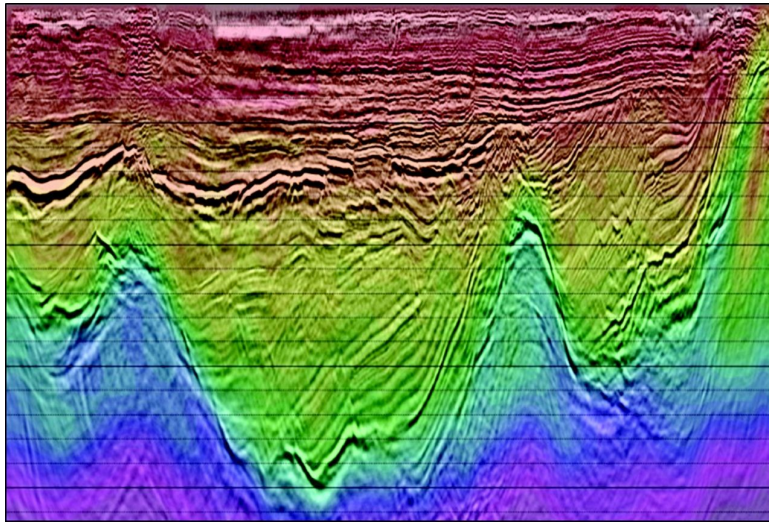


Thesis proposals on

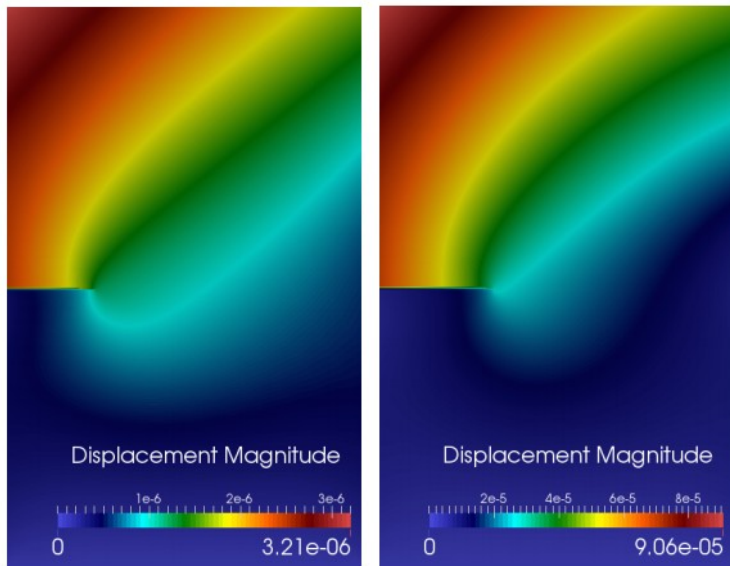
**Unfitted FEM for fractures and
inclusions in porous media**



Motivation

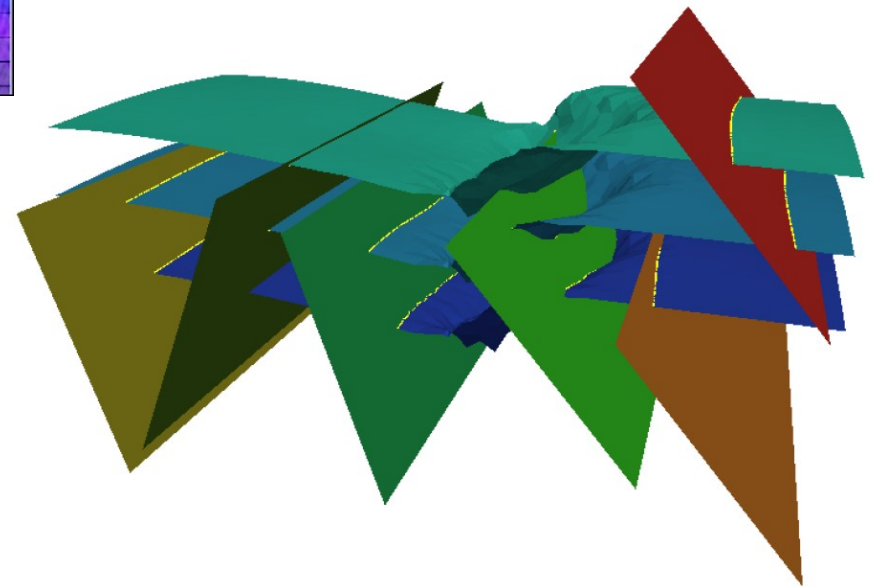


Complex geometries



$t = 0$

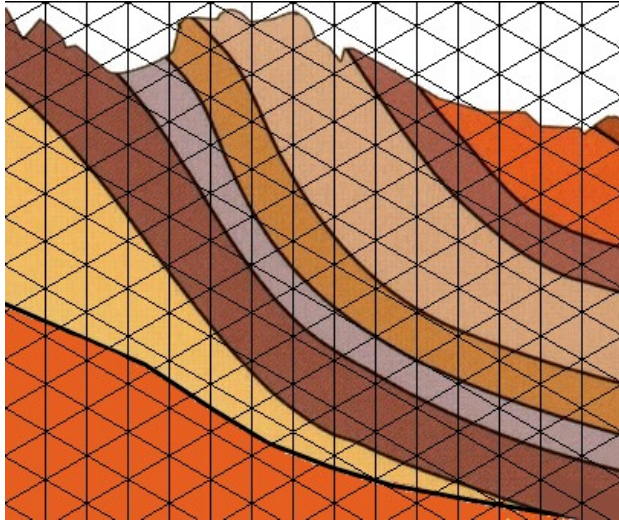
$t = 2 \text{ s}$



Uncertainty and moving interfaces

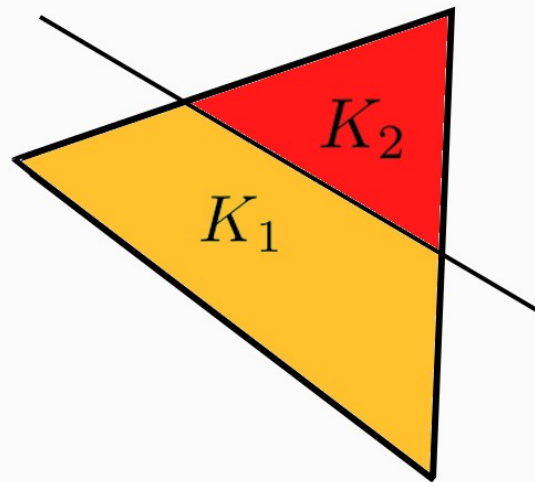


XFEM, GFEM, cutFEM...

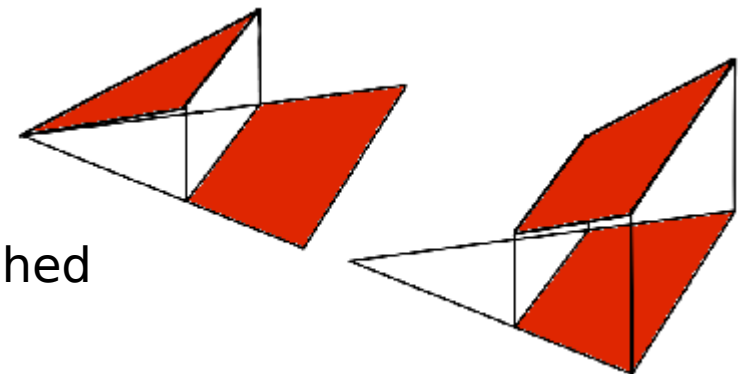


Heterogeneities/interfaces are not honored by the grid

Some grid elements have discontinuous coefficients or solutions inside



In these elements the standard FEM space is enriched with more DOFS/ ad hoc basis functions





Crack propagation

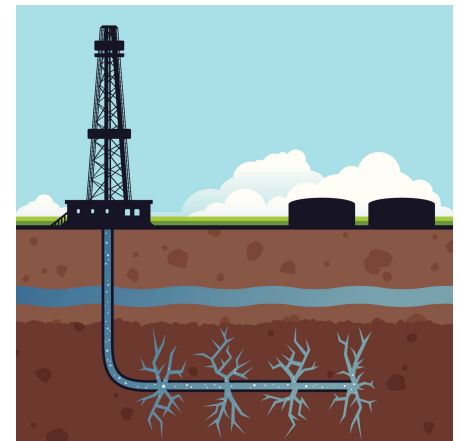
Un metodo innovativo per la propagazione di fratture, Correlatore B. Giovanardi

Motivation:

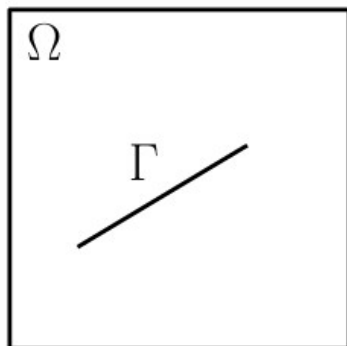


Failure due to
mechanical loading

Hydraulic fracturing



Governing equations:



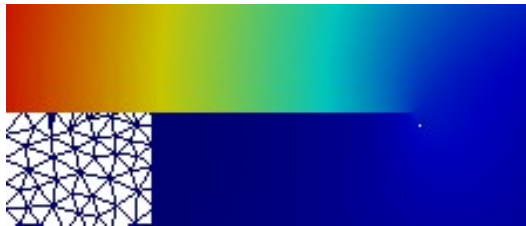
$$\left\{ \begin{array}{ll} \nabla \cdot \boldsymbol{\sigma} = \mathbf{0} & \text{in } \Omega \\ \boldsymbol{\sigma} \mathbf{n} = \mathbf{0} & \text{on } \Gamma, \\ + \text{B.C.} & \text{on } \partial\Omega \setminus \Gamma \end{array} \right.$$



A hybrid method

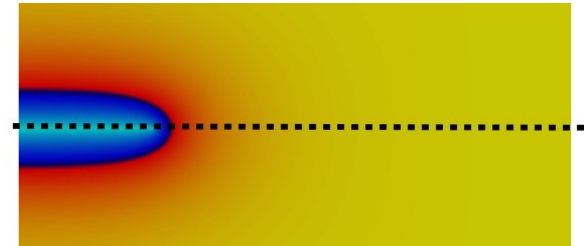
XFEM vs variational

XFEM methods allow the discontinuity of the displacement

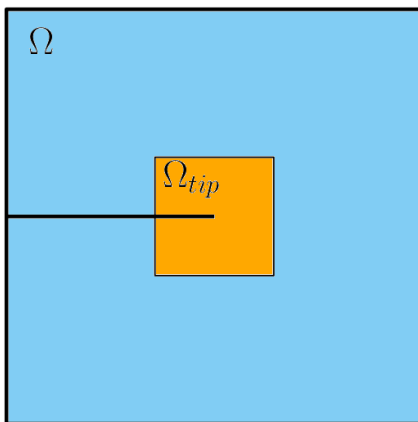


Needs extra criteria for crack propagation

A variable c varies continuously from the undamaged state, $c = 1$, to the cracked state, $c = 0$.



Crack propagation is “natural” (based on energy)



Solve **everywhere** using XFEM

Find BC for the local problem

Compute propagation with an energy based method (and a **fine mesh**) only where needed

Un metodo innovativo per la propagazione di fratture, Correlatore B. Giovanardi

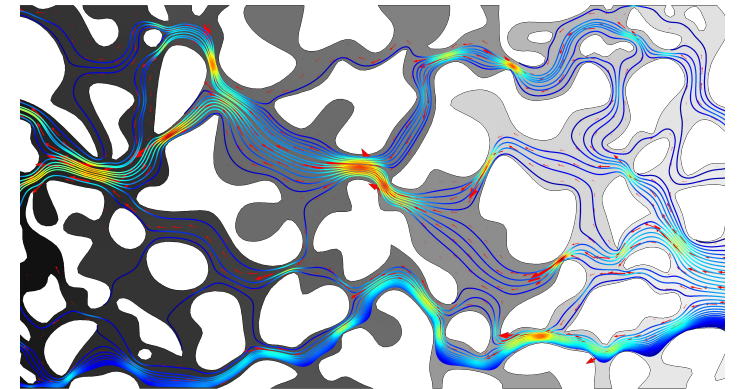


Stokes flow around a moving obstacle

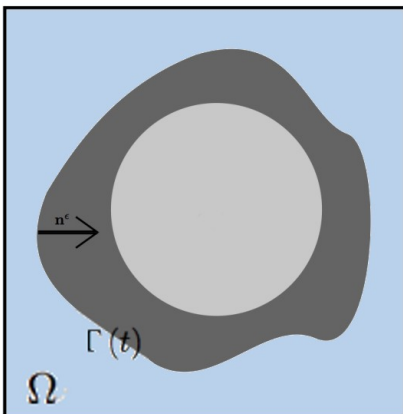
XFEM for unsteady Stokes' problem with moving interfaces, Correlatore P. Zunino

Motivation:

Pore scale flow in time dependent porous media (bio and geo applications)



Governing equations:



$$\begin{aligned} -\nabla \cdot (\mu \nabla \mathbf{u}) + \nabla p &= \mathbf{f} && \text{in } \Omega \\ \nabla \cdot \mathbf{u} &= 0 && \text{in } \Omega \end{aligned}$$

+BC

+ conditions on $\Gamma(t)$



Open issues

Model:

1) From an imposed geometry/motion of the interface to a fully coupled dynamic simulation

2) implicit representation of the interface by level set equations

Analysis:

1) time stepping vs space time FEM

2) Stability/stabilization of FEM spaces

Implementation:

Efficient implementation with variable DOF number

XFEM for unsteady Stokes' problem with moving interfaces, Correlatore P. Zunino